## Lab13-NPReduction CS363-Computability Theory, Xiaofeng Gao, Spring 2016

\* Please upload your assignment to FTP or submit a paper version on the next class \* If there is any problem, please contact: steinsgate@sjtu.edu.cn \* Name:\_\_\_\_\_ StudentId: \_\_\_\_\_ Email: \_\_\_\_\_

- 1. Find the certificate and certifier for the decision version of the following problems.
  - (a) Clique: Given an undirected graph, find a subset S that there is an edge connecting every pair of nodes in S with maximum nodes.
  - (b) Metric k-center: Given n cities with specified distances for each pair of cities as  $d_{ij}$ , one wants to build k warehouses in different cities and minimize the maximum distance of a city to a warehouse.
  - (c) Set Packing: Given a set U of n elements, a collection  $S_1, \dots, S_m$  of subsets of U, find the maximum subsets such that no two of them intersect.
  - (d) minimum k-cut: Given a weighted graph G = (V, E), we want to find a minimum weighted set of edges whose removal would partition the graph to k connected components.
- 2. The knapsack problem is a well-known optimization problem. Given a set of n items, each item i with a weight  $w_i$  and a value  $v_i$ , determine the number of each item to include in a collection so that the total weight is less than or equal to a given limit W and the total value is as large as possible.

Prove that the knapsack problem is NP-complete. (Hint: One solution is reducing the Subset Sum problem to it.)

- 3. We know that  $\mathbf{P} \subseteq \mathbf{NP} \cap \mathbf{co-NP}$ . Please give an example that belongs to following set. If you can, briefly explain your reason. (Should be examples different from the course slides).
  - (a) **Co-NP**.
  - (b) **Co-NP**  $\cap$  **NP-hard**.
  - (c) **Co-NP**  $\cap$  **NP**, but not known to be in **P**.