Query Optimization (I)

Spring, 2024

Overview

```
SELECT name, title
FROM instructor natural join teaches
    natural join course
WHERE dept_name ='Music';
```

- 1. Parse, check and verify the SQL
- 2. Translate into an RA query plan.
- 3. Query optimization: from an RA logical query plan to an optimized physical plan.

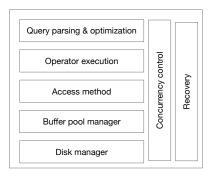
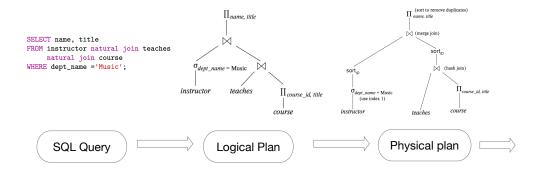


Figure: DBMS architecture

Agenda



- Rule-based query rewriting: find better logical plans via RA equivalence rules.
- Cost-based query optimization: cost estimation and optimal join order search

Query optimizer

- Recall that SQL is declarative.
 - Users specify what tuples they want.
 - The query optimizer searches and picks the best query plan.
- Cost difference between query plans for a query can be huge.
- The first query optimizer was implemented in System R, in the 1970s.
- Many concepts and design decisions from the System R optimizer are still used today.

P. Selinger et al. (1979). Access Path Selection in a Relational Database Management System.



Rule-based Query Rewriting

Basic equivalence rules

- $\bullet \ (i) \ R \bowtie S = S \bowtie R. \\ (ii) \ (R \bowtie S) \bowtie T = R \bowtie (S \bowtie T).$
 - Natural join is commutative and associative (except for attributes ordering).
- $\sigma_{\theta}(R \times S) = R \bowtie_{\theta} S$. This rule converts a cross product to a theta join.
- $\Pi_{L_1}(\Pi_{L_2}(R)) = \Pi_{L_1}(R)$, where $L_1 \subseteq L_2$.
- $\sigma_{\theta_1}(\sigma_{\theta_2}(R)) = \sigma_{\theta_1 \wedge \theta_2}(R)$.

Push down selection

Let θ_1 (resp. θ_2) be a predicate involving only attributes of R (resp. S). Then

$$\sigma_{\boldsymbol{\theta_1} \wedge \boldsymbol{\theta_2}}(R \bowtie_{\boldsymbol{\theta}} S) = \sigma_{\boldsymbol{\theta_1}}(R) \bowtie_{\boldsymbol{\theta}} \sigma_{\boldsymbol{\theta_2}}(S)$$

Intuition: Have fewer tuples in a plan.

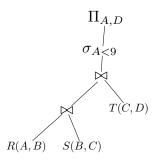
Push down projection

- 1. $\Pi_L(\sigma_{\theta}(R)) = \Pi_L(\sigma_{\theta}(\Pi_{L \cup L'}(R)))$
 - L' is the set of attributes that referenced by θ and not in L.
- 2. $\Pi_L(R \bowtie_{\theta} S) = \Pi_L(\Pi_{L'}(R) \bowtie_{\theta} S)$.
 - -L' consists of the set of attributes from R that either in L or referenced by θ .
- 3. A symmetric version of (2).

SQL query

```
-- R(A,B), S(B,C), T(C,D)
SELECT R.A, S.D
FROM R,S,T
WHERE R.B = S.B
AND S.C = T.C
AND R.A < 9;
```

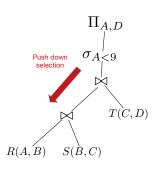
$$\Pi_{A,D}(\sigma_{A<9}((R\bowtie S)\bowtie T))$$



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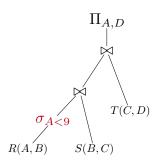
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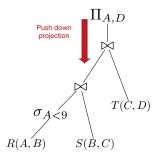
$$\Pi_{A,D}((\sigma_{A<9}(R)\bowtie S)\bowtie T)$$



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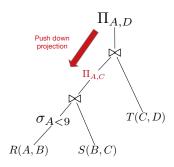
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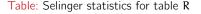


Cost estimation

- Plan cost = $\Sigma_{Operator \in Plan}$ (Operator cost)
- ullet Operator cost \propto Operator input size
- We have discussed how to estimate the cost of operators.
 - E.g., sequential/index scan, sort, joins.
- We still need to determine the size of operator input.
 - For base tables, it equals to the size on disk.
 - For other operators, it equals to "selectivity \times size of children."

Statistics and catalog

Notation	Statistics
R	number of tuples
P(R)	number of pages
NDV(A, R)	number of distinct values of A
max(A, R)	max value of A
min(A, R)	min value of A
H(A, R)	Tree index height of A





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- DBMS stores internal statistics about tables, attributes, and indexes in its internal catalog.
- Catalogs are updated periodically.
- Modern DBMS use much more sophisticated statistics.

P. Selinger et al. (1979). Access Path Selection in a Relational Database Management System.

Selection with equality predicates

$$\sigma_{A=\nu}(R)$$

- $|\sigma_{A=\nu}(R)| = |R|/NDV(A, R)$.
 - \circ |R|: the number of tuples in R.
 - NDV(A, R): the number of distinct values of A in R.
- Assumption: values of A are uniformly distributed in R.
- The selectivity factor of a predicate θ is the probability that a tuple in R satisfies θ .
- The selectivity factor of the predicate A = v is 1/NDV(A, R).

Conjunctive predicates

$$\sigma_{A=\nu \wedge B=u}(R)$$

- $|\sigma_{A=\nu \wedge B=u}(R)| = |R|/NDV(A, R) * NDV(B, R)$
- The selectivity factor of $A = \nu \wedge B = u$ is 1/NDV(A, R) * NDV(B, R).
- Additional assumption:
 - 1. A = v and B = u are independent;
 - 2. No over-selection, i.e., both A and B are not keys.

Negative and disjunctive predicates

$$\sigma_{A\neq\nu}(R)$$

- Selectivity factor for $A \neq v$ is 1 1/NDV(A, R).
- Selectivity factor $\neg \theta$ is (1 selectivity factor of θ).

$$\sigma_{A=\nu\vee B=u}(R)$$

- Selectivity factor: 1/NDV(A, R) + 1/NDV(B, R) 1/NDV(A, R) * NDV(B, R)
- Intuition: inclusion-exclusion principle.

Range predicates

$$\sigma_{A<\nu}(R)$$

- Suppose that min(A, R) and max(A, R) are available in catalog.
- If $v < \min(R, A)$, the selectivity factor is 0
- Otherwise, the selectivity factor is $\frac{\nu min(A,R)}{max(A-R) min(A,R)}$
- $\sigma_{A\geqslant \nu}(R)$ can be estimated symmetrically.

Join size estimation

$R(A, B) \bowtie S(B, C)$

- Estimate the size of the product of $R \times S$ as |R| * |S|.
- Take |R| * |S| / max(NDV(B, R), NDV(B, S)) as the join size estimation.
- Assumption: containment of value sets.
 - If NDV(B, R) < NDV(B, S), then $\Pi_B(R) \subseteq \Pi_B(S)$.
 - Not true in general. But holds in the common case of foreign key joins.
- Rationale
 - If NDV(B, R) < NDV(B, S), then each tuple in R joins with S/NDV(B, S) tuples of S.
 - Selectivity factor of R.B = S.B is 1/max(NDV(B, R), NDV(B, S)).

Join size estimation (cont'd)

Example

- |R| = 1000, |S| = 2000
- $\Pi(B, R) = 20$, $\Pi(B, S) = 50$.

Then $|R \bowtie S| = 1000 * 5000/max(20, 50) = 40000$.

Estimation error

- Lots of assumptions and very rough estimation.
- Skewness is one of the main reasons that may lead to bad estimations.
- The assumption of mutual independence of the predicates may not hold!

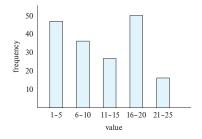
Example

Consider a table employee(id, level, salary).

- Let level \in (0, 10]. Then selectivity of level > 6 is estimated as $\frac{10-6}{10-0} = 40\%$.
- Real selectivity is significantly lower than 40%, e.g., 20%.
- Assume that selectivity of salary > 400000 is 30%. Then what is the selectivity of level > 6 ∧ salary > 400000 ?

Histograms

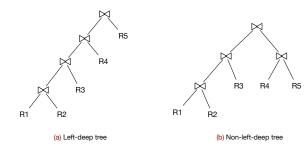
- Build histograms in the catalog to provide better estimation for common predicates over one or more columns.
- Equi-width: equal key ranges, store both key ranges and values.
- Equi-depth: histograms break up range such that each range has (approximately) the same number of tuples.
 - A equi-depth range example: (4, 8, 14, 19).



Cost-based plan search

- We have shown how to estimate the cost of one query plan.
- We next discuss how to pick the "best" one, i.e. the one with the lowest cost.
 - Enumerate all possible physical plans.
 - Pick the plan with the lowest cost.
- A piratical goal is often not getting the optimal plan, but avoiding the really bad ones.
- We will focus on the search of optimal join orders.

The search space for join order

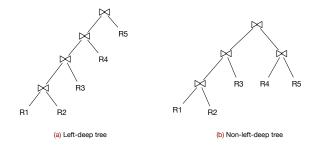


Recall that joins are commutative and associative.

(i)
$$R \bowtie S = S \bowtie R$$
. (ii) $(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$.

- The search plan of join orders can be huge.
- In general, there (2n-2)!/(n-1)! join orders for $R_1 \bowtie \cdots \bowtie R_n$.
 - When n = 6, (2n 2)!/(n 1)! = 30240.
 - When n = 10, (2n 2)!/(n 1)! > 17.6 billion.

Reduce search space



- In left-deep joins, only the left child can be a join operator.
- Left-deep joins allow to generate fully pipelined plans.
 - Intermediate results not written to temporary files.
 - Not all left-deep joins are fully pipelined, e.g., sort-merge join.
- There are n! different leaf-deep join trees for $R_1 \bowtie \cdots \bowtie R_n$.
 - \circ 6! = 720, 10! = 3628800
 - Significantly fewer, but still lots.

Selinger algorithm

- First implemented in System R, frequently adapted and used.
- Use Selinger statistics for cost estimation.
- Only consider left-deep joins for plan enumeration.
- Generate optimal plans in a bottom-up fashion.



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P. Selinger et al. (1979). Access Path Selection in a Relational Database Management System.

Dynamic programming

We find the optimal left-deep join order of $R_1, ..., R_n$ in a bottom-up fashion.

- Pass 1: Find the best single-table plan for $R_1, ..., R_n$.
- Pass 2: Find the best two-table plans for each pair of tables. This is done by combing best single table plans.
- ...
- Pass k: Find the best k-table plans for $\mathbb{S} \subseteq \{R_1, \dots, R_n\}$ with $|\mathbb{S}| = k$.

$$Opt_Cost(\mathbb{S}) = min_{R \in \mathbb{S}} \{Opt_cost(\mathbb{S} \setminus \{R\}) + Join_cost(\mathbb{S} \setminus \{R\}, R)\}$$

(i) Consider left-deep joins only. (ii) Pick the cheapest algorithm to join $(S \setminus \{R\})$ and R.

Optimal substructure property. Any subplan of an optimal join plan must also be optimal.

Dynamic programming (cont'd)

Subset	Best Plan	Cost
{ R }	SeqScan	100
{S}	SeqScan	80
{T}	IndexScan	50
{R, S}	HashJoin	260
{R, T}	MergeJoin	260
{S, T}	MergeJoin	240
$\{R, S, T\}$	HashJoin	700

Table: DP table for $R \bowtie S \bowtie T$

Cost analysis: $n * 2^n$:

- 2^n subsets in total and the size of each subset is at most n.
- \bullet For each subset $\mathbb S,$ it iterates through each element of $\mathbb S$ to find the optimal plan.

The need for interesting order

Subplan of the optimal plan is **not** optimal.

Example

 $R(A, B) \bowtie S(A, C) \bowtie T(A, D)$

- Best plan for $R \bowtie S$: hash join (beats sort-merge join).
- Best overall plan for $R \bowtie S \bowtie T$ can be
 - First Sort-merge join R and S
 - Then sort-merge join $R \bowtie S$ with T.

This can happen assuming that T is sorted on attribute A.

- An intermediate result has an interesting order if it is sorted by anything that can be exploited by later processing.
 - $\,\circ\,$ The result of the sort-merge join of R and S is sorted on A.
 - $\,\circ\,$ This is an interesting order since a subsequent merge join of $R\bowtie S$ and T can utilize it.

Dealing with interesting orders

Subset	Best Plan	Interesting order	Cost
 {R, S} {R, S}	 HashJoin MergeJoin 	 Ø {A}	 160 200

Table: DP table for $R(A, B) \bowtie S(A, C) \bowtie T(A, D)$ with interesting order

- When picking the best plan
 - Comparing their cost is not enough
 - Comparing interesting orders is also needed
- Computes multiple optimal plans for each subset, one for each interesting order.
- Increases the complexity by factor k + 1, where k is the number of interesting orders.

Recap

- Rule-base query rewriting
 - Relational algebra equivalence rules
- Cost-based optimization
 - Need statistics to estimate sizes of intermediate results.
 - Dynamic programming for join orderings.

In practice, query optimization can be much more challenging.

Moerbotte and Neumann. Dynamic Programming Strikes Back. SIGMOD '08 $\,$