

# Computer Graphics

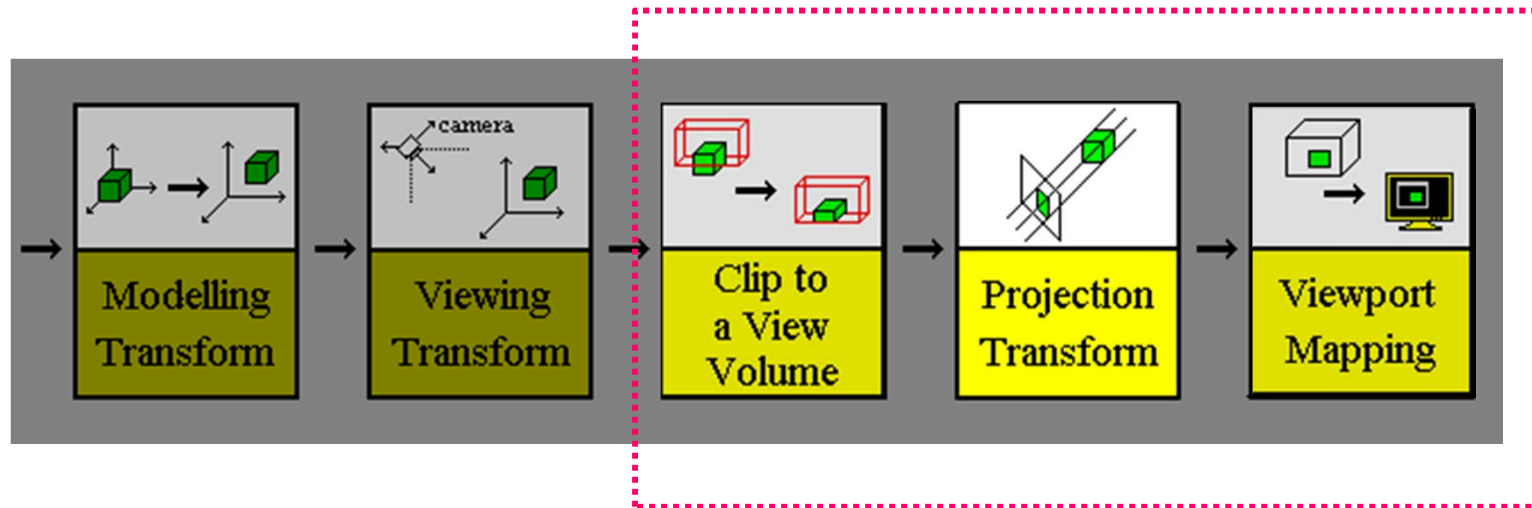
## Chapter 8 (I)

### Two - Dimensional Viewing

# Outline

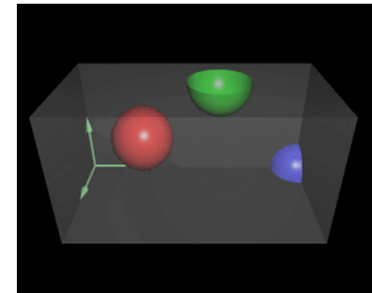
- Viewing Pipeline
- World Coordinates Transfer to Viewing Coordinates
- Normalization and Viewport Transformations
- OpenGL 2D Viewing Functions
- OpenGL 2D Viewing Program Example

# Viewing Pipeline



# Viewing Volume

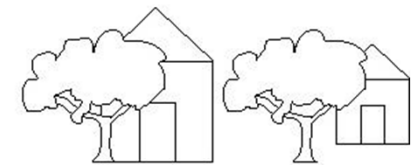
- Viewing volume
  - A closed volume which delimits the **infinite** 3D space to **finite** volume.
  - Points outside it will not appear on the screen.
- Two projections to create viewing volume
  - Orthographic projection
    - Objects rendered are not affected by the distance
    - E.g.: a menu, a text on a screen, 2D objects...
  - Perspective projection
    - Objects rendered are affected by the distance
    - E.g.: a car is seen smaller when it move away



Orthographic



Perspective

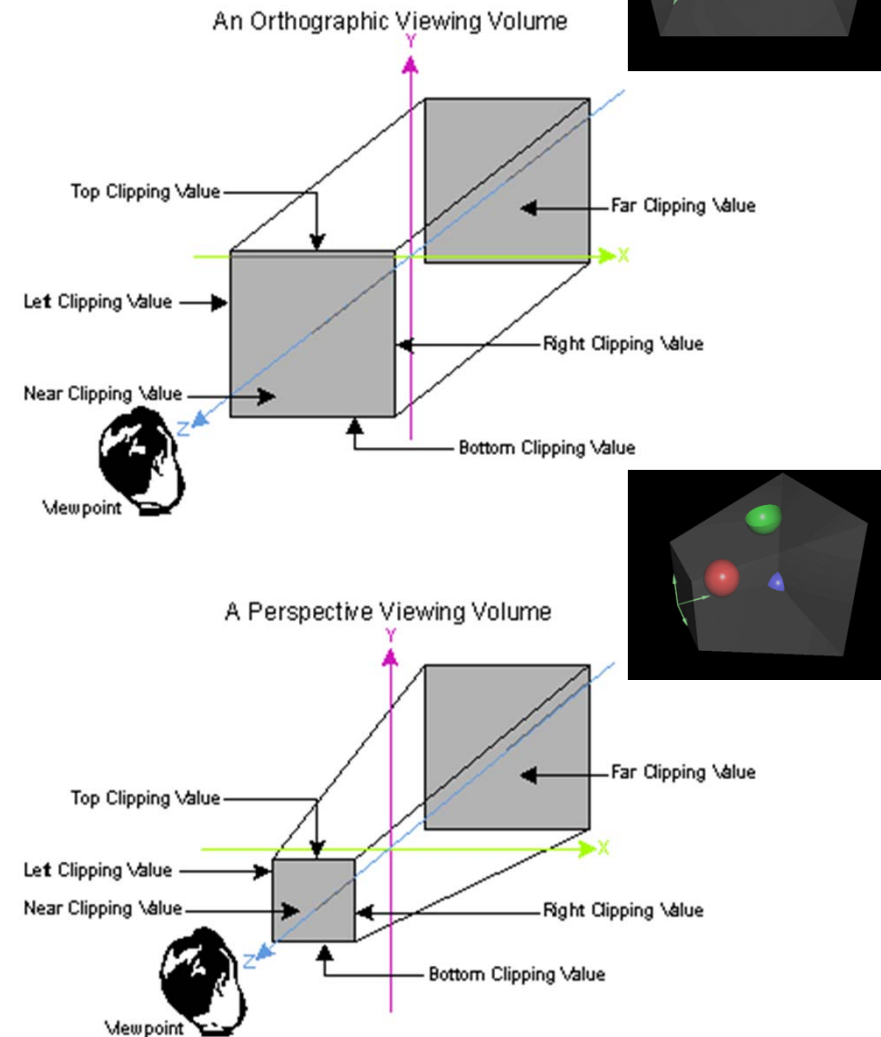


Orthographic

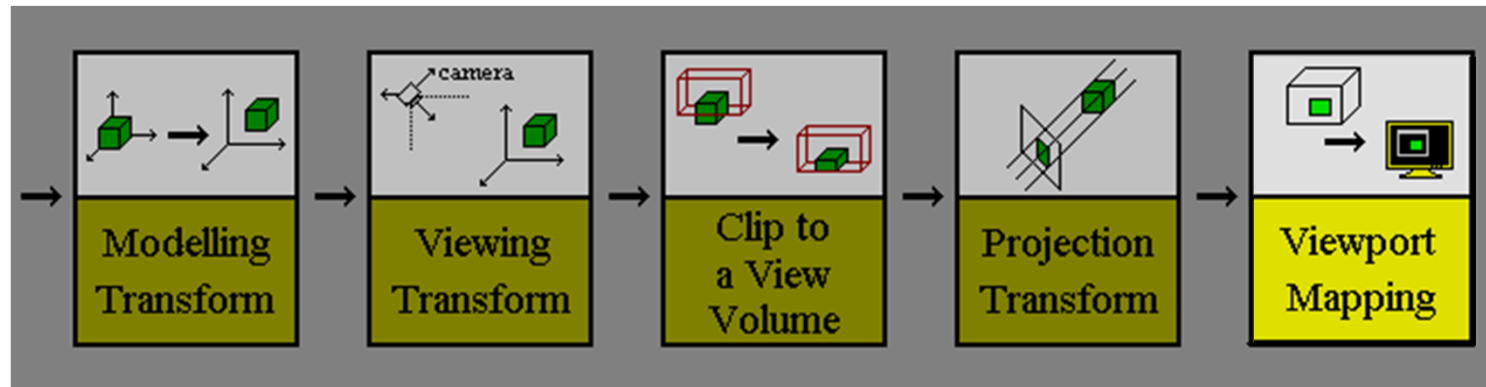
Perspective

# Viewing Volume

- Orthographic projection
  - Viewing volume shape is a parallelepiped(平行六面體).
  - Parallel clipping planes
- Perspective projection
  - Viewing volume shape is a truncated pyramid (its top is cut).
  - Non-parallel side clipping planes



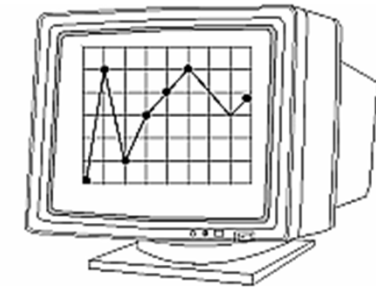
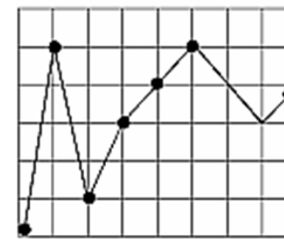
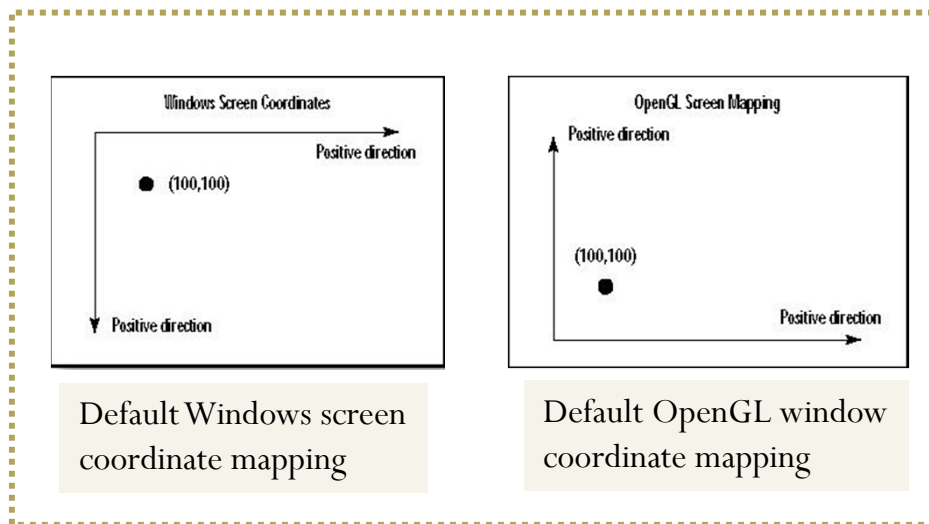
# Viewport



- Viewport
  - 2D drawing region of the screen where the final result is mapped.

# Viewport

- Measured in actual window coordinates



( From OpenGL Super Bible)

`void glViewport (GLint x, GLint y, GLsizei width, GLsizei height);`

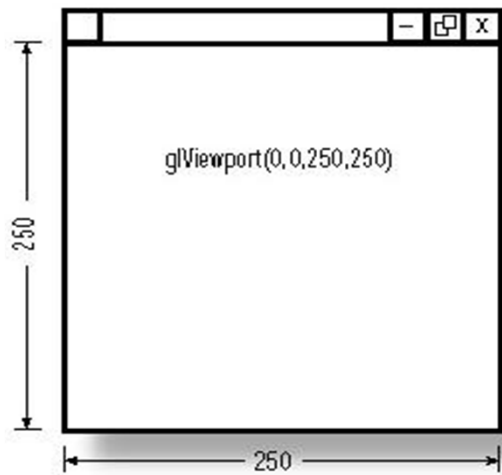
*(x, y)*: specifies the lower-left corner of the viewport;

*width* and *height*: the size of the viewport rectangle.

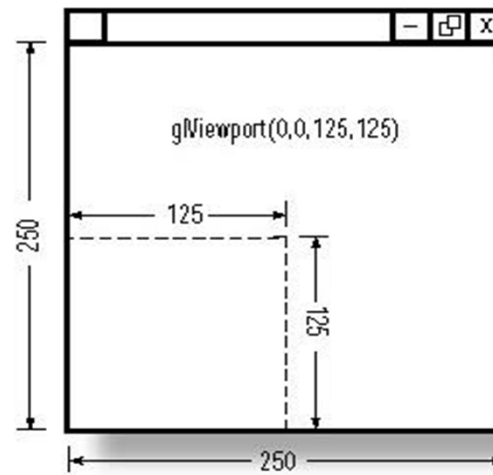
**By default**, the initial viewport are `(0, 0, winWidth, winHeight)`, where *winWidth* and *winHeight* are the size of the window.

# Viewport

- Example



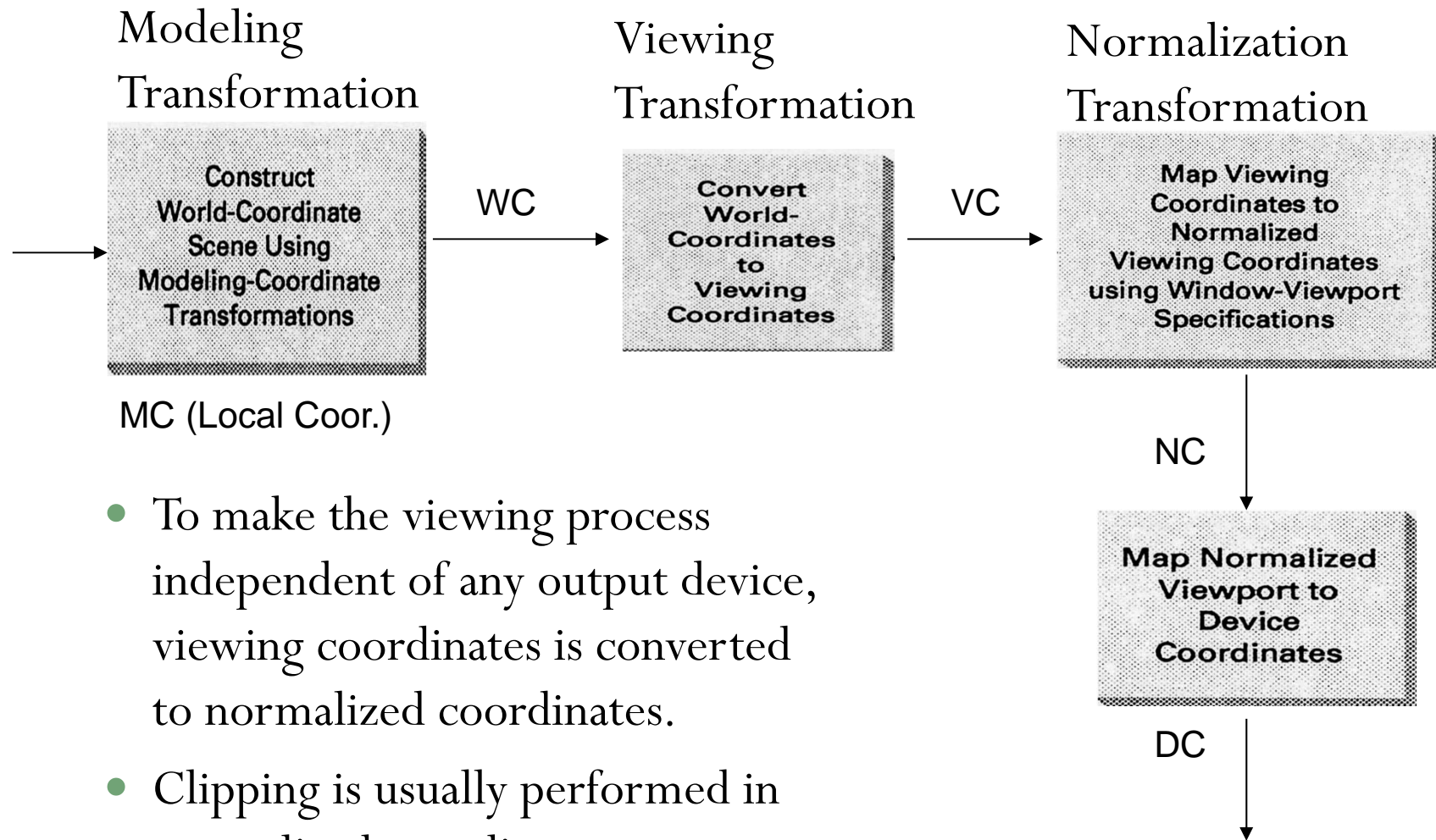
Window and viewport are same



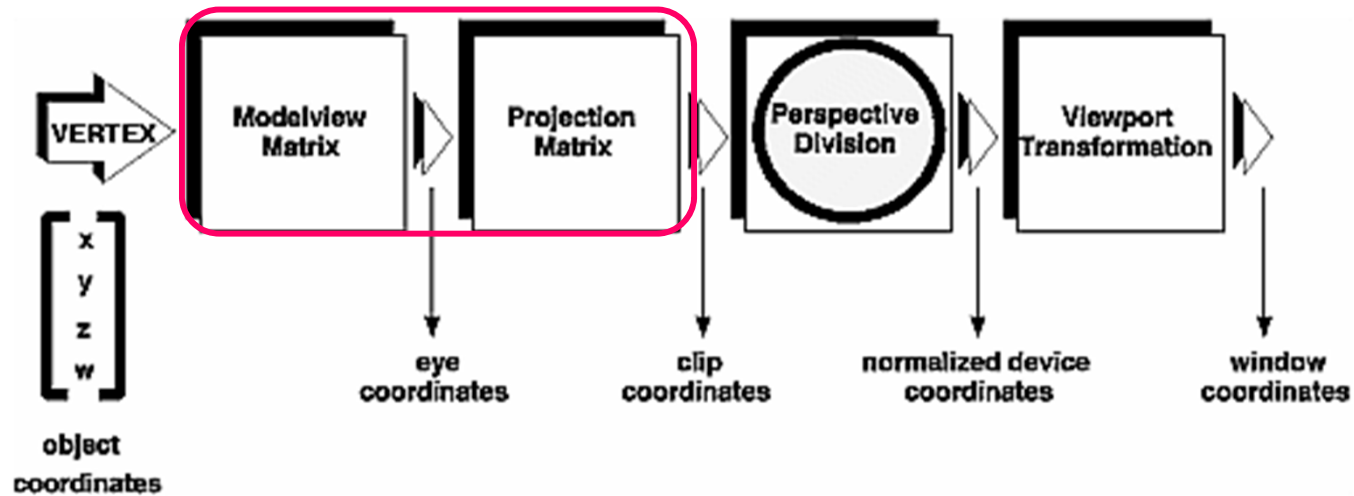
Viewport 1/2 size of window



# 2D Viewing Pipeline

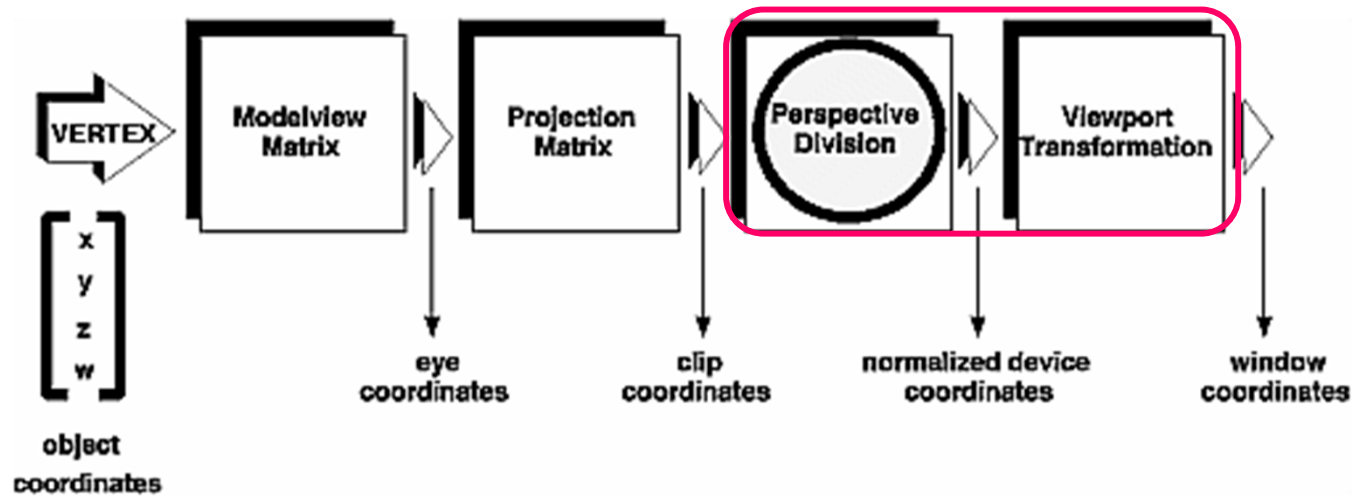


# Stages of Vertex Transformation



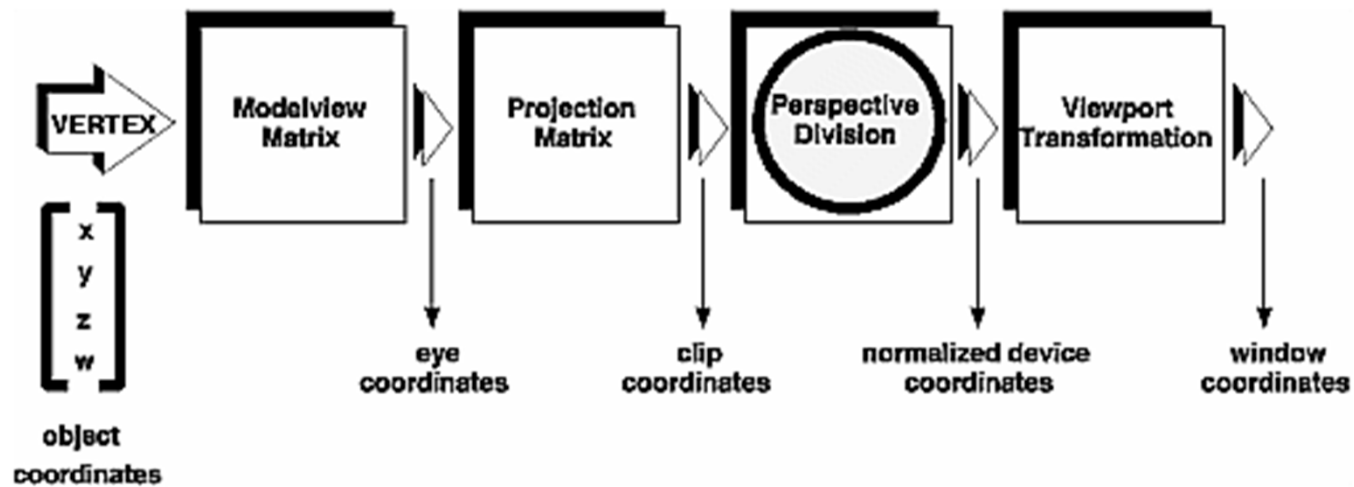
- Matrix-form in OpenGL
  - The **viewing** and **modeling** transformations you specify are combined to form the **modelview** matrix, which is applied to the incoming *object coordinates* to yield **eye (viewing) coordinates**.
  - The **projection** matrix to yield **clip coordinates**.
    - Defines a viewing volume

# Stages of Vertex Transformation



- Matrix form in OpenGL (cont.)
  - The *perspective division* is performed by dividing coordinate values by  $w$ , to produce *normalized device coordinates*.
  - The transformed coordinates are converted to *window coordinates* by applying the viewport transformation.
    - You can specify the size of the viewport to cause the final image result.

# Stages of Vertex Transformation

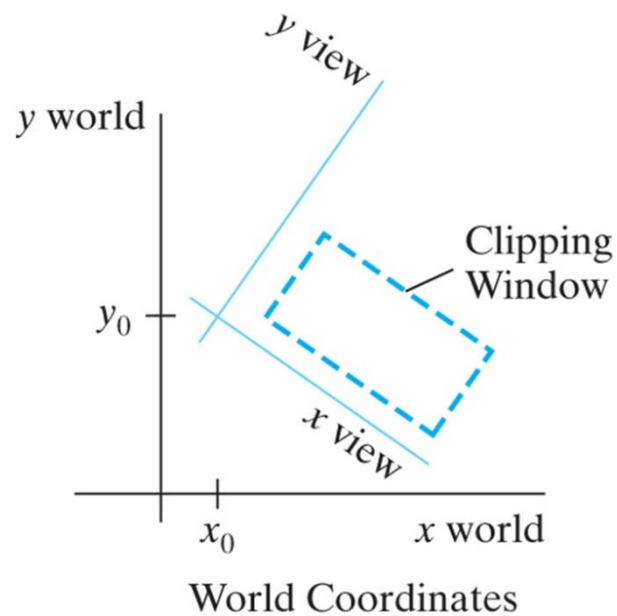


- The viewing, modeling, and projection transformations matrix in OpenGL:  $4 \times 4$  **matrix  $M$**  [in 2D,  $z = 0$ ]
- They are multiplied by the coordinates of each vertex  $v$  in the scene

$$v' = Mv$$

# World Coordinates Convert to Viewing Coordinates

We can set up a 2D viewing coordinate system in the world coordinate frame.



$(x_0, y_0)$ : an origin

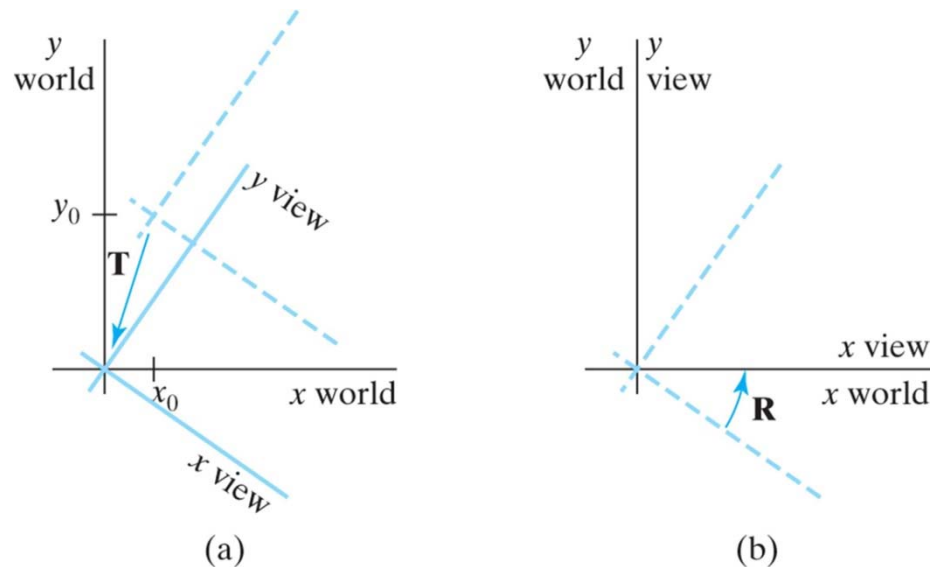
yview: 2D view up vector

This viewing coordinate frame provides a reference for specifying the clipping window.



**Fig. 8-3** A rotated world window in *Viewing Coordinates*.

# World Coordinates Convert to Viewing Coordinates



$$\mathbf{M}_{wc \rightarrow vc} = \mathbf{R} \cdot \mathbf{T} \quad (8-1)$$

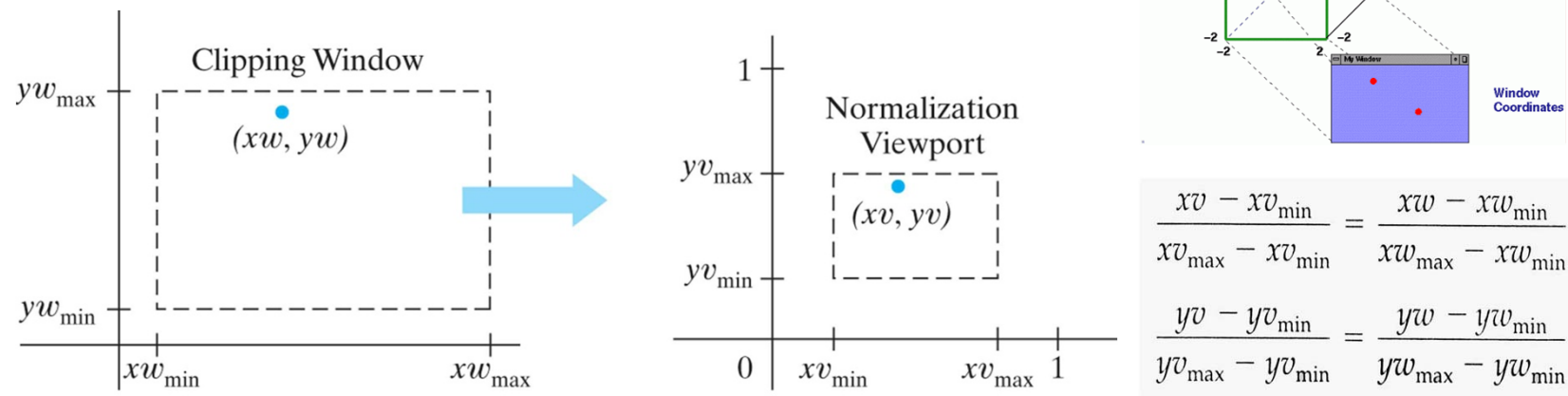
Where  $\mathbf{T}$  is the translation matrix that takes the viewing origin point  $P_0$  to the world origin, and  $\mathbf{R}$  is the rotation matrix that aligns the axes of the two reference frames

**FIGURE 8-4** A *Viewing-Coordinate* frame is moved into coincidence with the *World - Coordinate* frame by

- (a) applying a **translation** matrix  $\mathbf{T}$  to move the viewing origin to the world origin, then
- (b) applying a **rotation** matrix  $\mathbf{R}$  to align the axes of the two systems.

# Normalization and Viewport Transformations

- Mapping a clipping window into a normalized viewport  
(the viewport is given within  $( [0, 1], [0, 1] )$  )



**FIGURE 8-6** A point  $(xw, yw)$  in a world-coordinate clipping window is mapped to viewport coordinates  $(xv, yv)$ , within a unit square, so that the relative positions of the two points in their respective rectangles are the same.

# OpenGL 2D Viewing Functions

- OpenGL Projection Mode

```
glMatrixMode (GL_PROJECTION); //projection matrix  
glLoadIdentity ();
```

- GLU Clipping-Window Function

```
gluOrtho2D (xwmin, xwmax, ywmin, ywmax);  
2D parallel projection.
```

- OpenGL Viewport Function

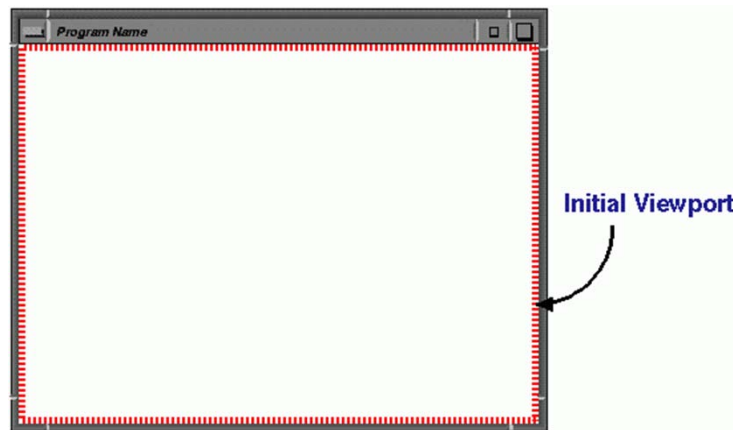
```
glViewport (xvmin, yvmin, vpWidth, vpHeight);  
glGetIntegerv (GL_VIEWPORT, vpArray);
```

To obtain the parameters for the currently active viewport: xvmin, yvmin, vpWidth, vpHeight.

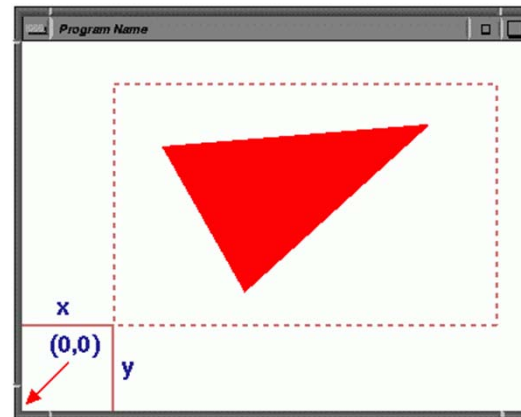


# OpenGL Viewport Function

- `glViewport (GLint x, GLint y, GLsizei width, GLsizei height);`



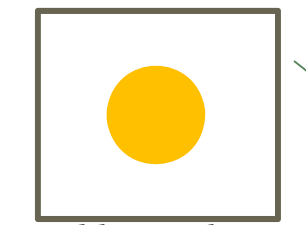
You can change it by `glViewport()`.



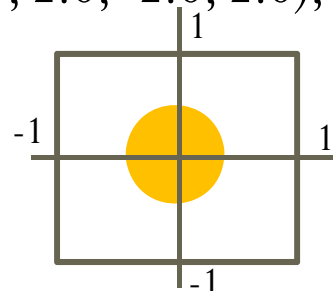
Always rectangle;

$x, y$  are in window coordinates

- Example: `gluOrtho2D (-2.0, 2.0, -2.0, 2.0);`

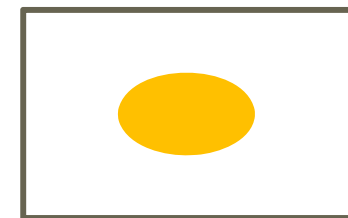


World Coordinates



Normalized Device Coordinates

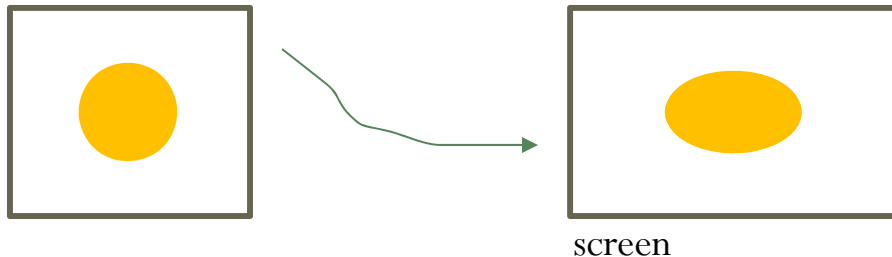
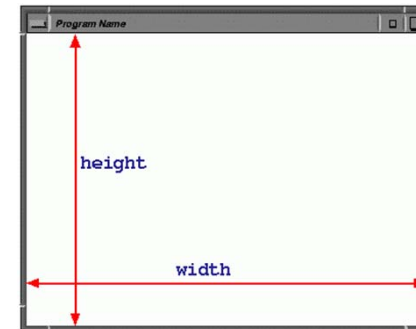
`glViewport (0, 0, 300, 150);`



Window Coordinates

# OpenGL Viewport Function

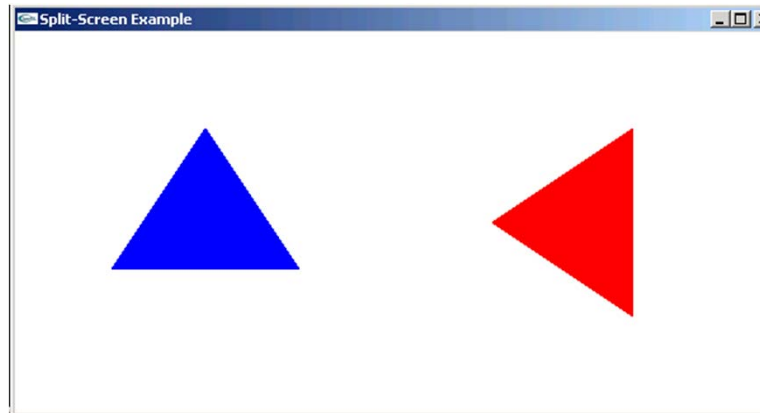
- The rectangle area has an aspect ratio: width / height
  - Windows
    - `glutInitWindowSize ( width, height );`
  - 2D clipping window
    - `gluOrtho2D ( left, right, bottom, top );`
  - Viewport
    - `glViewport ( x, y, width, height);`
- In general, the clipping window (viewing volume) and viewport need to have the same ratio.



# OpenGL 2D Viewing Program Example

- Two views of a triangle in the  $xy$  plane shown in a split screen, with its centroid at the world-coordinate origin

```
#include <GL/glut.h>
class wcPt2D
{
public:
    GLfloat x, y;
};
```



# OpenGL 2D Viewing Program Example

```
void init (void)
{
    /* Set color of display window to white. */
    glClearColor (1.0, 1.0, 1.0, 0.0);

    /* Set parameters for world-coordinate clipping window. */
    glMatrixMode (GL_PROJECTION);
    gluOrtho2D (-100.0, 100.0, -100.0, 100.0);

    /* Set mode for construction geometric transformation matrix. */
    glMatrixMode (GL_MODELVIEW);
}
```

# OpenGL 2D Viewing Program Example

```
void triangle (wcPt2D *verts)
{
    GLint k;

    glBegin (GL_TRIANGLES);
        for (k =0; k < 3; k++)
            glVertex2f (verts [k].x, verts [k].y);
        glEnd ();
}
```

# OpenGL 2D Viewing Program Example

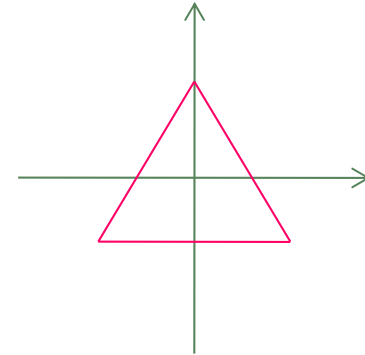
```
void displayFcn (void)
{
    /* Define initial position for triangle. */
    wcPt2D verts [3] = { {-50.0, -25.0}, {50.0, -25.0}, {0.0, 50.0} };

    glClear (GL_COLOR_BUFFER_BIT);    // Clear display window.

    glColor3f (0.0, 0.0, 1.0);        // Set fill color to blue.
    glViewport (0, 0, 300, 300);    // Set left viewport.
    triangle (verts);                 // Display red rotated triangle.

    /* Rotate triangle and display in right half of display window. */
    glColor3f (1.0, 0.0, 0.0);        // Set fill color to red.
    glViewport (300, 0, 300, 300);    // Set right viewport.
    glRotatf (90.0, 0.0, 0.0, 1.0);    // Rotate about z axis.
    triangle (verts);                 // Display red rotated triangle.

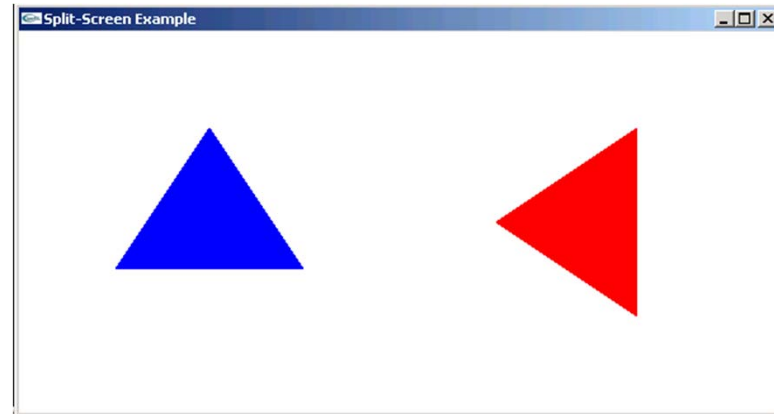
    glFlush (); //Force to execute all OpenGL functions
}
```



# OpenGL 2D Viewing Program Example

```
void main (int argc, char **argv)
{
    glutInit (&argc, argv);
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);
    glutInitWindowPosition (50, 50);
    glutInitWindowSize (600, 300);
    glutCreateWindow ("Split-Screen Example");

    init();
    glutDisplayFunc (displayFcn);
    glutMainLoop ();
}
```



# OpenGL 2D Viewing Functions

- You need to handle the changes in the window size
  - Registering a window reshape callback
    - `void glutReshapeFunc ( void (*func) (int width, int height) );`
  - Defining the reshape callback function: pass the new width and height of the window
    - called before the first call to the display function,
    - and called automatically when the window is reshaped.
    - e.g. `MyReshape ()`;

```
void MyReshape ( int width, int height )
{
    /* update viewport */
    glViewport (...);
    /* reset viewing volume */
    glMatrixMode ( GL_PROJECTION);
    glLoadIdentity();
    gluOrtho2D (...);
    /* set modelview matrix mode
    ...
}
```



# Summary

- 2D viewing pipeline
- OpenGL 2D viewing functions